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Mining with Multi-objective Evolutionary
Optimization: Implicit and Explicit Function
Representations Mixing Unsupervised and
Supervised Properties *

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Virtual Reality Spaces for Visual Data Mining with Multiobjective Evolutionary Optimization: Implicit and Explicit Function Representations Mixing Unsupervised and Supervised Properties

Julio J. Valdés and Alan J. Barton,

Abstract-Multi-objective optimization is used for the computation of virtual reality spaces for visual data mining and knowledge discovery. Two methods for computing new spaces are discussed: implicit and explicit function representations. In the first, the images of the objects are computed directly, and in the second, universal function approximators (neural networks) are obtained. The pros and cons of each approach are discussed, as well as their complementary character. The NSGA-II algorithm is used for computing spaces requested to minimize two objectives: a similarity structure loss measure (Sammon's error) and classification error (mean cross-validation error on a k-nn classifier). Two examples using solutions along approximations to the Pareto front are presented: Alzheimer's disease gene expressions and geophysical fields for prospecting underground caves. This approach is a general non-linear feature generation and can be used in problems not necessarily oriented to the construction of visual data representations.

I. INTRODUCTION

The role of visualization techniques in the knowledge discovery process is well known. The increasing complexity of the data analysis procedures makes it more difficult for the user to extract useful information out of the results generated by the various techniques. This makes graphical representation directly appealing. Data and patterns should be considered in a broad sense. There are different kinds of data (relational, graphical, symbolic, etc.). An example of a heterogeneous database is shown in Fig. 1. The increasing rates of data generation require the development of procedures facilitating the *understanding* of the structure of this kind of data more rapidly and intuitively.

Virtual Reality (VR) is a suitable paradigm for visual data mining. It is *flexible*: allows the choice of different ways how to represent the objects according to the differences in human perception. VR allows *immersion*: the user can navigate inside the data and interact with the objects in the world. It creates a *living* experience: the user is a passive observer, but an actor in the world. VR is *broad and deep*: the user may see the VR world as a whole, or concentrate on details. Very important is that its use does not require any special background. A virtual reality technique for visual

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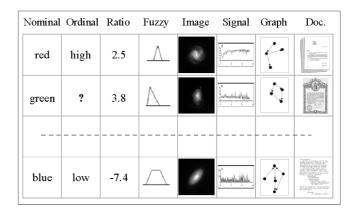


Fig. 1. An example of a heterogeneous database. Nominal, ordinal, ratio, fuzzy, image, signal, graph, and document data are mixed. The symbol? denotes a missing value.

data mining on heterogeneous, imprecise and incomplete information systems was introduced in [17], [18].

One of the steps in the construction of a VR space for data representation is the transformation of the original set of attributes describing the objects under study, often defining a heterogeneous high dimensional space, into another space of small dimension (typically 2-4) with intuitive metric (e.g. Euclidean). The operation usually involves a non-linear transformation; implying some information loss. There are basically two kinds of spaces sought: i) spaces preserving the structure of the objects as determined by the original set of attributes, and ii) spaces preserving the distribution of an existing class defined over the set of objects. Since in many cases the set of descriptor attributes does not necessarily relate well with the decision attribute, both types of spaces are usually conflicting. Moreover, they are created by different non-linear transformations. This situation creates confusion, because the same set of objects has a different distribution and different properties in two separate spaces. It would be better to construct spaces where several criteria could be simultaneously covered and with a unique metric.

This paper explores the construction of VR spaces for visual data mining using multi-objective optimization based on genetic algorithms (MOGA) and implicit and explicit function representations. This approach provides solutions for the previously discussed problems and the possibility of obtaining sets of spaces in which several properties (objectives) are expressed in different degrees. This strategy

is a conceptual improvement w.r.t. computing spaces using single-objective optimization algorithms in which the objective function is a weighted composition of different criteria. The possibility of computing either implicit or explicit mappings based on the same principles adds flexibility and the possibility of choosing the mapping strategy best suited for the type of problem and data.

This approach is illustrated with two real world problems: the representation of a very high dimensional genomics dataset (Alzheimer's disease gene expressions), and the study of the effectiveness of a given set of geophysical fields in detecting the presence of underground caves.

II. VIRTUAL REALITY REPRESENTATION OF RELATIONAL STRUCTURES

A visual, data mining technique based on virtual reality oriented to general relational structures was introduced in [17], [18], (see also http://www.hybridstrategies.com). It is oriented to the understanding of large heterogeneous, incomplete and imprecise data, as well as symbolic knowledge. The notion of data is not restricted to databases, but includes logical relations and other forms of both structured and non-structured knowledge.

Different information sources are associated with the attributes, relations and functions. They are described by the so called source sets (Ψ_i) , constructed according to the nature of the information to represent. Source sets also account for incomplete information.

Definition 1: A heterogeneous domain [19] is a Cartesian product of a collection of source sets: $\hat{\mathcal{H}}^n = \Psi_1 \times \cdots \times \Psi_n$, where n > 0 is the number of information sources to consider. For example, in a domain where objects are described by continuous crisp quantities, discrete features, fuzzy features, time-series, images, and graphs, they can be represented as Cartesian products of subsets of real numbers(\hat{R}), nominal (\hat{N}) or ordinal sets(\hat{O}), fuzzy sets(\hat{F}), sets of images (\hat{I}) , sets of time series (\hat{S}) and sets of graphs (\hat{G}) , respectively (all extended to allow missing values, indicated by $\hat{}$). The heterogeneous domain is $\hat{\mathcal{H}}^n = \hat{N}^{n_N} \times$ $\hat{O}^{n_O} \times \hat{R}^{n_R} \times \hat{F}^{n_F} \times \hat{I}^{n_I} \times \hat{S}^{n_S} \times \hat{G}^{n_G}$, where n_N is the number of nominal sets, n_O of ordinal sets, n_R of real-valued sets , n_F of fuzzy sets , n_I of image-valued sets, n_S of time-series sets, and n_G of graph-valued sets, respectively $(n = n_N + n_O + n_R + n_F + n_I + n_S + n_G).$

Definition 2: A virtual reality space is the tuple $\Upsilon = < Q, G, B, \Re^m, g_o, l, g_r, b, r>$, where Q is a relational structure $Q = < O, \Gamma^v>$, Q is a finite set of objects, and Γ^v is a set of relations); Q is a non-empty set of geometries representing the different objects and relations; Q is a non-empty set of behaviors of the objects in the virtual world; Q is a metric space of dimension Q (euclidean or not) which will be the actual virtual reality geometric space. The other elements are mappings: Q is Q is Q is Q is Q is Q if Q is Q.

A. A Taxonomy of the Virtual Reality Spaces

If the objects are in a heterogeneous space, $l: \hat{\mathcal{H}}^n \to \Re^m$. Several desiderata can be considered for building a transformed space either for constructing visual representations or as new generated features for pattern recognition purposes. The property which the objects in the space must satisfy, the mapping can be:

- *Unsupervised*: The location of the objects in the space should preserve some structural property of the data, dependent only on the set of descriptor attributes. Any class information is ignored. The space sought should have minimal distortion.
- Supervised: The goal is to produce a space where the objects are maximally discriminated w.r.t. a class distribution. The preservation of any structural property of the data is ignored, and the space can be distorted as much as required in order to maximize class discrimination.
- Mixed: A space compromising the two goals is sought.
 Some amount of distortion is allowed in order to exhibit class differentiation and the object distribution should retain in a degree the structural property defined by the descriptor attributes. Very often these two goals are conflicting.

From the point of view of their mathematical nature, the mappings can be:

- *Implicit*: the images of the transformed objects are computed directly and the algorithm does not provide a function representation.
- *Explicit*: the function performing the mapping is found by the procedure and the images of the objects are obtained by applying the function. Two sub-types are:
 - *analytical functions*: for example, as an algebraic representation.
 - *general function approximators*: for example, as neural networks, fuzzy systems, or others.

Explicit mappings can be constructed in the form of analytical functions (e.g. via genetic programming), or using general function approximators like neural networks or fuzzy systems. An explicit l is useful for both practical and theoretical reasons. On one hand, in dynamic data sets (e.g. systems being monitored or incremental data bases) an explicit transform l will speed up the update of the VR information space. On the other hand, it can give semantics to the attributes of the VR space, thus acting as a general dimensionality reducer.

B. The unsupervised perspective: Structure preservation

Data structure is one of the most important elements to consider and this is the case when the location and adjacency relationships between the objects O in Υ should give an indication of the *similarity relationships* [3], [1] between the objects in $\hat{\mathcal{H}}^n$, as given by the set of original attributes [19]. l can be constructed to maximize some metric/non-metric structure preservation criteria as has been done for decades in multidimensional scaling [12], [1], or to minimize some error measure of information loss [15]. If δ_{ij} is a dissimilarity

measure between any two $i, j \in U$ $(i, j \in [1, N],$ where N is the number of objects), and $\zeta_{i^v j^v}$ is another dissimilarity measure defined on objects $i^v, j^v \in O$ from Υ (i^v = $\xi(i), j^v = \xi(j)$, examples of error measures frequently used

S stress =
$$\sqrt{\frac{\sum_{i < j} (\delta_{ij}^2 - \zeta_{ij}^2)^2}{\sum_{i < j} \delta_{ij}^4}}$$
, (1)
Sammon error = $\frac{1}{\sum_{i < j} \delta_{ij}} \frac{\sum_{i < j} (\delta_{ij} - \zeta_{ij})^2}{\delta_{ij}}$ (2)
Quadratic Loss = $\sum_{i < j} (\delta_{ij} - \zeta_{ij})^2$ (3)

Sammon error =
$$\frac{1}{\sum_{i < j} \delta_{ij}} \frac{\sum_{i < j} (\delta_{ij} - \zeta_{ij})^2}{\delta_{ij}}$$
(2)

Quadratic Loss =
$$\sum_{i < j} (\delta_{ij} - \zeta_{ij})^2$$
 (3)

Classical algorithms have been used for directly optimizing these measures, like Steepest descent, Conjugate gradient, Fletcher-Reeves, Powell, Levenberg-Marquardt, and others. The number of different similarity, dissimilarity and distance functions definable for the different kinds of source sets is immense. Moreover, similarities and distances can be transformed into dissimilarities according to a wide variety of schemes, thus providing a rich framework. In particular, for heterogeneous data involving mixtures of nominal and ratio variables, the Gower similarity measure [9] has proven to be suitable. This similarity between objects i and j is given by

$$S_{ij} = \sum_{k=1}^{p} s_{ijk} / \sum_{k=1}^{p} w_{ijk}$$
 (4)

If $v_k(i), v_k(j)$ are the values of attribute k for objects i and j respectively, an invalid comparison occurs when at least one them is missing. For quantitative attributes, the scores s_{ijk} are assigned as $s_{ijk} = 1 - |v_k(i) - v_k(j)|/R_k$, where R_k is the range of attribute k. For nominal attributes $s_{ijk} = 1$ if $v_k(i) = v_k(j)$, and 0 otherwise. The weight (w_{ijk}) of the attribute k is set equal to 0 if the comparison is invalid or 1 otherwise.

If Eqs-1-2-3 are optimized by setting the collection of coordinates in the new space as the unknowns of the error measures the l mappings are implicit, as functional representations are not obtained. When 3D spaces with Euclidean metric are targeted, the genetic algorithms can use linear realvalued chromosomes . Their length is set to $N \cdot M$ where Nis the number of objects and M the dimension of the new space (Fig. 2). Thus, each chromosome represents the result of an implicit mapping $l: \mathbb{R}^N \to \mathbb{R}^M$.

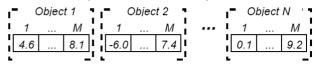
C. The supervised perspective: Class Separability

In the supervised case, a natural choice for representing the l mapping is a non-linear discriminant analysis neural network (NDA) [23], [11]. One strong reason is that classes are often either only separable with nonlinear boundaries, or not separable at all. Another is the generalization capability of neural networks which allows the placement of new unseen objects. When learning the mapping the neural network last hidden layer creates new nonlinear features for the mapped objects, such that they are separated into classes by the output

Real Valued Chromosome Representation

4.6 2.6 8.1 -6.0 1.9 7.4 1.3 3.1 5.8 0.1 8.4 9.2

VR Space Chromosome Representation



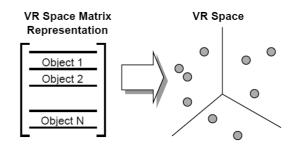


Fig. 2. Chromosome representation for the multi-objective optimization.

layer. These nonlinear features could be used independently by other data mining algorithms. The typical architecture of such networks is shown in Fig. 3.

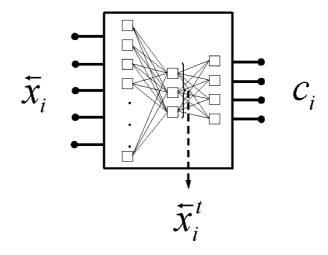


Fig. 3. Feed forward neural network for 2-objective optimization. \vec{x}_i is an input pattern to the network, c_i is the network-predicted class membership of the input vector as coded by the output network layer and \vec{x}_i^t is the output of the last hidden layer, representing a transformation of the input vector into another space.

The number of input nodes is set to the number of features of the data objects, and the number of neurons in the output layer to be the number of pattern classes, whereas the number of neurons in the last hidden layer (m) is the dimensionality of the new space. Since the classical approach to building NDA networks suffers from the known problem of local extrema entrapment, the construction of NDA networks can be done by using hybrid stochastic-deterministic feed forward networks where training is based on a combination of simulated annealing with conjugate gradient [13] [21]. Alternatively, networks based on evolutionary algorithms can use, for instance, genetic algorithms, or particle swarm optimization combined with classical optimization techniques as proposed in [20].

D. The multi-objective approach: A hybrid perspective

The relationship between the original descriptor variables and the class membership may be partial, or poor. Thus, a space that satisfactorily preserves the similarity structure does not necessarily maximize class separability. If classification is all that matters, then it can be achieved at the cost of distorting the space much more than another one compliant with the similarity structure. In so doing, the kind and amount of nonlinearity and distortion introduced may be so large that the data distribution in the two spaces may bear no resemblance at all. These two goals are usually in conflict and multi-objective optimization can bring a new perspective to the problem. In a first approximation, the minimization of a measure of similarity information loss between the original and the transformed spaces and a classification error measure over the objects in the new space can be used as objectives. More requirements can be imposed on the solution by adding the corresponding objective functions. This paper will consider the use of only two criteria: Sammon's error (Eq-2) for the unsupervised case and mean cross-validated classification error with a k-nearest neighbour pattern recognizer for the supervised case using Euclidean distance.

III. MULTI-OBJECTIVE OPTIMIZATION USING GENETIC ALGORITHMS

An evolutionary algorithm constructs a population of individuals, which evolve through time until stopping criteria is satisfied. At any particular time, the current population of individuals represent the current solutions to the input problem, with the final population representing the algorithm's resulting output solutions.

An enhancement to the traditional evolutionary algorithm, is to allow an individual to have more than one measure of fitness within a population. One way in which such an enhancement may be applied, is through the use of, for example, a weighted sum of more than one fitness value [2]. MOGA, however, offers another possible way for enabling such an enhancement. In the latter case, the problem arises for the evolutionary algorithm to select individuals for inclusion in the next population because a set of individuals contained in one population exhibits an approximation to a Pareto Front [14] – hereafter called the locus of the non-dominated solutions (LNDS) – of best current individuals, rather than a single best individual. Most [2] multi-objective algorithms use the concept of dominance.

A solution $\overline{x}_{(1)}$ is said to dominate [2] a solution $\overline{x}_{(2)}$ for a set of m objective functions $< f_1(\overline{x}), f_2(\overline{x}), ..., f_m(\overline{x}) >$ if

1) $\overline{x}_{(1)}$ is not worse than $\overline{x}_{(2)}$ over all objectives. For example, $f_3(\overline{x}_{(1)}) \leq f_3(\overline{x}_{(2)})$ if $f_3(\overline{x})$ is a minimization objective.

2) $\overline{x}_{(1)}$ is strictly better than $\overline{x}_{(2)}$ in at least one objective. For example, $f_6(\overline{x}_{(1)}) > f_6(\overline{x}_{(2)})$ if $f_6(\overline{x})$ is a maximization objective.

One particular algorithm for MOGA is the elitist nondominated sorting genetic algorithm (NSGA-II) [4], [5], [6], [2]. It has the features that it i) uses elitism, ii) uses an explicit diversity preserving mechanism, and iii) emphasizes the non-dominated solutions. The procedure is as follows: i) Create the child population using the usual genetic algorithm operations. ii) Combine parent and child populations into a merged population. iii) Sort the merged population according to the non-domination principle. iv) Identify a set of fronts in the merged population $(\mathcal{F}_i, i = 1, 2, ...)$. v) Add all complete fronts \mathcal{F}_i , for i = 1, 2, ..., k - 1 to the next population. viThere may now be a front, \mathcal{F}_k , that does not completely fit into the next population. So select individuals that are maximally separated from each other from the front \mathcal{F}_k according to a crowding distance operator. vii) The next population has now been constructed, so continue with the genetic algorithm operations.

IV. A MULTI-OBJECTIVE IMPLICIT MAPPING EXAMPLE

This approach is illustrated with gene expression data from a genomic research on Alzheimer's disease. Alzheimer's disease (AD) is an incurable chronic, progressive, debilitating condition which, along with other neurodegenerative diseases, represents the largest area of unmet need in modern medicine. A total of 12 samples from clinically diagnosed AD patients and 11 from "normal" patients of similar age were used in this study. Each sample is characterized by a 9600 attributes describing expression intensities of a corresponding number of genes [22]. Clearly, direct inspection of the structure of this 9600-dimensional data, and of the relationship between the descriptor variables (the genes) and the class (Normal or Alzheimer), is impossible. The need for a visual representation respecting at the same time the object interrelationships as defined by the 9600 genes and the class differentiation, makes this problem suitable for a MOGA approach. The collection of parameters describing the application of the NSGA-II algorithm is shown in Table-I. A modest population size and number of generations were used, with a relatively high mutation probability in order to enable richer genetic diversity. Randomization of the set of data objects was applied in order to reduce the bias in the composition of the cross-validated folds by providing a more even class distribution between successive training and test subsets. The number of folds was set in consideration of the sample size.

The set of non-dominated solutions obtained by the NSGA-II algorithm is shown in the scatter plot of Fig. 4, where the horizontal axis is the mean cross-validated knn error and the vertical axis the Sammon error. The approximate location of the Pareto front is defined by the convex polygon joining the solutions provided by chromosomes 0, 3, 2, 4, 1 (Table-II). Chromosome 0 defines a space with a perfect resolution of the supervised problem in terms of the

population size	100	
number of generations	200	
chromosome length	69	
ga seed	4001	
objective functions should be	minimized	
chromosome data representation	real	
crossover probability	0.8	
crossover type	uniform (prob. 0.6)	
mutation probability	0.4	
mutation type	gaussian	
selection type	tournament	
tournament probability	0.6	
perform mutation and crossover	yes	
population initialization	random, bounded	
lower bound for initialization	0	
upper bound for initialization	7	
fitness values	raw objective values	
stopping criteria	maximum iterations	
restart ga during execution	no	
number of objectives	2	
number of constraints	0	
pre-computed diss. matrix	Gower dissimilarity	
evaluation functions	mean cross-validated error	
	Sammon error	
cross-validation (c.v.)	5 folds	
randomize before c.v.	yes	
knn seed	-101	
k nearest neighbors	3	
non-linear mapping measure	Sammon	
dimension of the new space	3	

Normal and Alzheimer classes (knn error = 0), but at the cost of a severe distortion of the space. Whereas, chromosome 1 approximates a pure unsupervised solution (with low Sammon error). Its classification error is large indicating that few non-linear features preserving the similarity structure lacks classification power. This may be due to the large amount of attribute noise, redundancy, and irrelevancy within the set of 9600 original genes.

TABLE II
SELECTED MULTI-OBJECTIVE SOLUTIONS

multi-objective	mean cross-validation	Sammon error
GA solution	k-nn error	
chromosome 0	0.0000	1.1712
chromosome 3	0.0500	0.8900
chromosome 2	0.0800	0.6924
chromosome 4	0.1700	0.5480
chromosome 1	0.3100	0.4926

Clearly, it is impossible to represent virtual reality spaces on a static medium. However, a composition of snapshots of the VR spaces using the solutions along the LNDS is shown in Fig. 5.a-5.e. For comparison Fig. 5.f corresponds to an unsupervised single-objective solution obtained with deterministic optimization (Newton's method) using Sammon's error (Eq-2), Gower's similarity in the original space (Eq-4), and normalized Euclidean metric in the new space was obtained in [22]. The error obtained was 0.1034 after 335 iterations. This error is much better than the equivalent

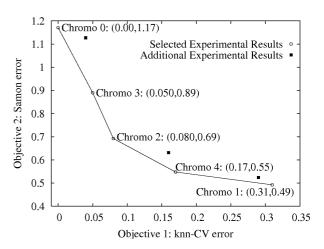


Fig. 4. Different solutions along the LNDS progressively spanning the extremes given by minimum classification error, and minimum dissimilarity loss. The errors corresponding to the two objective functions are shown in parenthesis.

MOGA result (error = 0.49), obtained with a reduced number of generations a small population size, which considerably reduces the search space. However, the space defined by chromosome 1 (Fig. 5.e) captures most of the features of the purely unsupervised solution obtained with deterministic methods and a much larger number of iterations. This indicates the potential room for improvement of the MOGA results. Chromosome 2, according to Fig. 4 and Fig. 5.c, can be considered to be the best MOGA compromised solution in which both error criteria are simultaneously as low as possible. It shows a reasonable class discrimination with a non-large similarity structure distortion, which is a very meaningful result.

V. A MULTI-OBJECTIVE EXPLICIT MAPPING EXAMPLE

Here a explicit representation in the form of a neural network will be constructed, although from a MOGA perspective. The output of the neural network is used for obtaining a classification, and the output of the last hidden layer is used for computing Sammon error (Fig. 3).

This approach was applied to geophysical data in an investigation about the detection of underground caves. Sometimes they are opened to the surface, but typically they are buried, requiring the use of geophysical methods. Cave detection is a very important problem in civil and geological engineering. The studied area contained an accessible cave and geophysical methods complemented with a topographic survey were used with the purpose of finding their relation with subsurface phenomena [16]. This is a problem with partially defined classes: the existance of a cave beneath a measurement station is either known for sure or unknown (i.e. only one class membership is defined).

The set of geophysical methods included 1) the spontaneous electric potential (SP) at the earths surface measured in the dry season, 2) the vertical component of the electromagnetic field in the very low frequency region of the

electromagnetic spectrum, 3) the SP in the rainy season, 4) the gamma radioactive intensity and 2) the local topography.

In order to eliminate the data distortion introduced by the different units of measure for the physical fields, to reduce the influence of noise and regional geological structures a data preprocessing process was performed consisting of several steps: i) conversion of each physical field to standard scores. ii) each physical field f was modeled as composed of a trend, a signal and additive noise: f(x,y) = t(x,y) + s(x,y) + n(x,y) where t is the trend, s is the signal, and n is the noise component. iii) a least squares linear trend $\hat{t}(x,y) = c_0 + c_1 x + c_2 x + c_3 x + c_4 x + c_5 x +$ c_2y , was estimated, and a residual obtained: $\hat{r}(x,y) =$ $f(x,y) - \hat{t}(x,y)$. The residual was convolved with a low pass two-dimensional filter to attenuate the noise component: $\hat{s}(x,y) = \sum_{k_1=-N}^{N} \sum_{k_2=-N}^{N} h(k_1,k_2) \hat{r}(x-k_1,y-k_2),$ where $\hat{r}(x,y)$ is the residual, $\hat{s}(x,y)$ is the signal approximation, and $h(k_1, k_2)$ is the low-pass zero-phase shift digital filter. The filtered residuals fields were clustered using the leader algorithm [10] and the parameters shown in Table-III. As a result, 648 leaders (cluster representatives) were found from the 1225 original objects. They retain most of the original similarity structure because of the high threshold value.

TABLE III

EXPERIMENTAL SETTINGS FOR i) THE INPUT DATA ii) THE LEADER ALGORITHM, iii) THE EVOLUTIONARY MULTI-OBJECTIVE OPTIMIZATION ALGORITHM (NSGA-II), AND iv) THE OBJECTIVE FUNCTIONS (E.G. THE NON-LINEAR DISCRIMINANT ANALYSIS).

225
variant: closest
Gower
).97
348
100
2000
Determined by NN layout
Exp-1: 816, 523
Exp-2: 325, 617
Exp-3: 192, 893
0.8
0.4
Minimize (for all objectives)
Jniform, prob.= 0.6
Gaussian
Fournament, prob.= 0.6
ves .
-100, 100 per allele
Raw
After max. iterations
No
Classification Error and
Sammon Error
hidden layer (3 neurons)
output layer (2 neurons)
anh for both layers
)

A series of MOGA experiments were performed. The experimental settings are shown in Table-III, which comprise

a description of the data, the leader algorithm options, the MOGA options, and the two objective function parameters, including the parameters used for non-linear discriminant analysis.

Each MOGA experiment generate approximately 10 distinct multi-criteria solutions, which lead to a total of approximately 30 distinct solutions for the multi-criteria problem. Fig. 6 shows the solutions and the resulting LNDS.

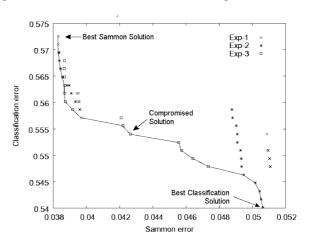


Fig. 6. Different multi-objective solutions for the geophysical prospecting example, with an approximation to the Pareto front.

Three solutions were selected from Fig. 6 that represent the two extremes and a compromise of these two objectives. These selections were then each visualized by constructing a 3-dimensional VR space from the hidden layer of the neural network solutions as shown in Fig. 7. The representation at the top in Fig. 7 shows the best MOGA Sammon error solution, with the property of preserving data structure. While the bottom representation shows the best MOGA classification error solution; a space in which objects should be maximally separated in terms of their class membership (cave or unknown). The middle representation demonstrates a MOGA compromised solution exhibiting intermediate properties of the two extreme solutions.

VI. CONCLUSIONS

MOGA was applied to the computation of virtual reality spaces for visual data mining, using implicit and explicit function representations. In both cases MOGA solutions range from purely unsupervised solutions to purely supervised, providing a variety of spaces s.t. each one fulfills these properties in different degree within a single metric. Implicit solutions are more suitable when the number of objects is reduced, the number of attributes is large and only the visualization of a single sample is needed. When the number of objects is large, the number of attributes not so large and new objects besides those covered by the sample are expected, explicit solutions are appropriate. The effectiveness of a MOGA approach was shown with examples from genomics and geophysical prospecting. A more thorough experimental study of this approach is necessary across other domains in order to assess the technique's general behaviour.

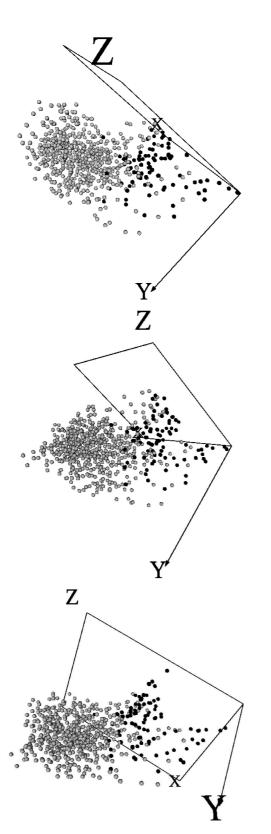


Fig. 7. Selected MOGA solutions. Top: best Sammon error solution. Middle: Solution compromising both error measures. Bottom: best classification error solution. Dark objects represent measuring stations over the known surveyed cave location. Light objects represent measuring stations where the existance of a cave is unknown.

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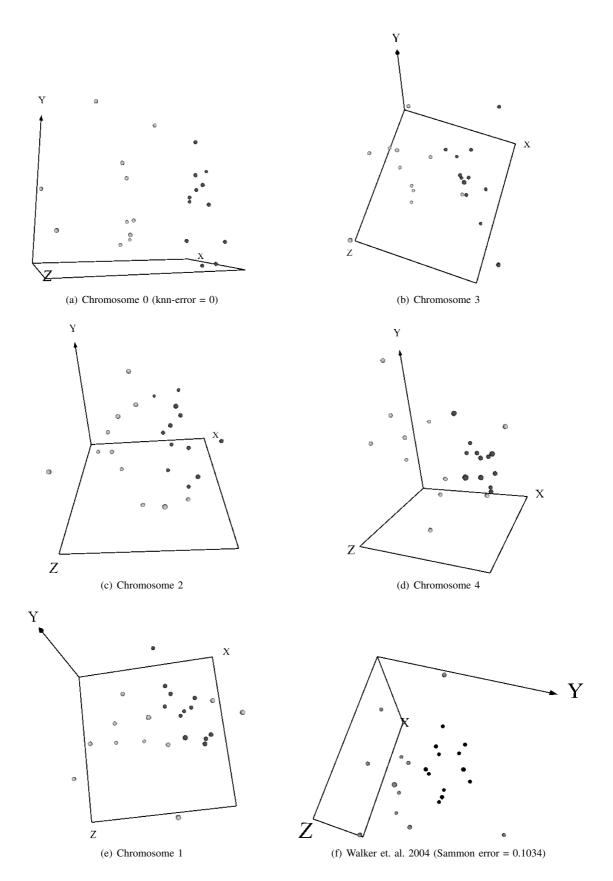


Fig. 5. Snapshots of vr-spaces computed with different solutions along the LNDS progressively spanning the extremes given by minimum classification error, and minimum dissimilarity loss. Light spheres = normal samples, dark spheres = Alzheimer samples.